22206

21718 3 Hours / 70 Marks

Seat No.

Instructions : (1) All Questions are *compulsory*.

- (2) Answer each next main Question on a new page.
- (3) Figures to the right indicate full marks.
- (4) Use of Non-programmable Electronic Pocket Calculator is permissible.
- (5) Mobile Phone, Pager and any other Electronic Communication devices are not permissible in Examination Hall.

Marks

1. Attempt any FIVE of the following :

(a) State whether the function $f(x) = \frac{a^x + a^{-x}}{2}$ is even or odd.

(b) If
$$f(x) = x^2 + 6x + 10$$
, find $f(2) + f(-2)$.

(c) If
$$y = \log (x^2 + 2x + 5)$$
, find $\frac{dy}{dx}$.

(d) Evaluate :
$$\int \frac{1}{\sin^2 x \cos^2 x} dx$$
.

- (e) Find the area enclosed by the curve $y = 3x^2$, x-axis and the ordinates x = 1, x = 3.
- (f) An unbiased coin is tossed 5 times. Find the probability of getting a head.
- (g) Evaluate : $\int x \cos x \, dx$.

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2. Attempt any THREE of the following :

(a) If
$$e^x + e^y = e^{x+y}$$
, find $\frac{dy}{dx}$.

(b) If
$$x = a(\theta + \sin \theta)$$
, $y = a(1 - \cos \theta)$, find $\frac{dy}{dx}$ at $\theta = \frac{\pi}{2}$.

- (c) Find the maximum and minimum values of $y = 2x^3 3x^2 36x + 10$.
- (d) A telegraph wire hangs in the form of a curve $y = a \log \left(\sec \left(\frac{x}{a} \right) \right)$ where 'a' is constant. Show that radius of curvature at any point is a sec $\left(\frac{x}{a} \right)$.

3. Attempt any THREE of the following :

- (a) Find the equation of tangent and normal to the curve $y = 2x x^2$ at (2, 0).
- (b) Differentiate $(\sin x)^{\tan x}$ w.r.t. x.

(c) If
$$Y = \sqrt{\frac{1 - \cos 2x}{1 + \cos 2x}}$$
, find $\frac{dy}{dx}$.

(d) Evaluate :
$$\int \frac{\sin \sqrt{x}}{\sqrt{x}} dx$$
.

4. Attempt any THREE of the following :

(a) Evaluate :
$$\int \frac{1}{\sqrt{1-x^2}(\sin^{-1}x)^2} dx$$

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(b) Evaluate :
$$\int \frac{1}{5+4\cos x} dx$$

(c) Evaluate :
$$\int \frac{x}{1 + \cos 2x} \, \mathrm{d}x$$

(d) Evaluate :
$$\int \frac{\sec^2 x}{(1 + \tan x)(2 + \tan x)}$$

(e) Evaluate :
$$\int_{0}^{\pi/2} \frac{\sqrt[3]{\sin x}}{\sqrt[3]{\cos x} + \sqrt[3]{\sin x}} dx$$

5. Attempt any TWO of the following :

- (a) Find the area of the region bounded by the parabola $y = 4x x^2$ and the x-axis.
- (b) Attempt the following :
 - (i) Form the D.E. by eliminating the arbitrary constants if

 $y = A \cos 3x + B \sin 3x.$

- (ii) Solve : $x(1 + y^2)dx + y(1 + x^2)dy = 0$.
- (c) A particle starting with velocity 6 m/sec has an acceleration $(1 t^2)$ m/sec², when does it first come to rest ? How far has it then travelled ?

6. Attempt any TWO of the following :

(a) Attempt the following :

(i) A person fires 10 shots at target. The probability that any shot will hit the target 3/5. Find the probability that the target is hit exactly 5 times.

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- (ii) If 20% of the bolts produce by a machine are defective. Find the probability that out of 4 bolts drawn,
 - (1) one is defective.
 - (2) at the most two are defective.
- (b) A company manufacture electric motors. The probability that an electric motor is defective is 0.01. What is the probability that a sample of 300 electric motors will contains exactly 5 defective motors ? (Given $e^{-3} = 0.0498$)
- (c) In a sample of 1000 cases the mean of certain test is 14 and standard deviation is 2.5. Assuming the distribution to be normal, find
 - (1) how many students score above 18?
 - (2) how many students score between 12 and 15?

[Given : A(0.4) = 0.1554, A(0.8) = 0.2881, A(1.6) = 0.4452]