



MAHARASHTRA STATE BOARD OF TECHNICAL EDUCATION

(Autonomous)

(ISO/IEC-270001 – 2005 certified)

WINTER-2014 EXAMINATION

Subject code: 17421

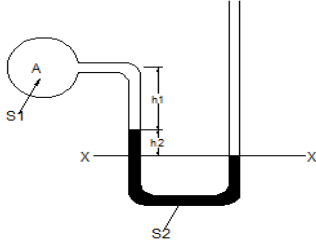
Model Answer

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Important Instructions to examiners:

- 1) The answer should be examined by keywords and not as word-to-word as given in the model answer scheme.
- 2) The model answer and the answer written by candidate may vary but the examiner may try to assess the understanding level of the candidate.
- 3) The language error such as grammatical, spelling errors should not be given more importance. (Not applicable for subject English and communication skill).
- 4) While assessing figures, examiner may give credit for principal components indicated in the figure. The figure drawn by candidate and model answer may vary. The examiner may give credit for any equivalent figure drawn.
- 5) Credits may be given step wise for numerical problems. In the some cases, the assumed constants values may vary and there may be some difference in the candidates answer and model answer.
- 6) In case of some questions credit may be given by judgment on part of examiner of relevant answer based on candidates understanding.

Q1 Attempt any TEN of the following	20
a) Define mass density & state its SI unit.	
Mass Density:- The mass density of a liquid may be defined as the mass per unit volume at standard temperature.	01
SI unit :- kg/m^3	01
b) State four application of Hydraulics in environmental engineering.	
Ans:- Four applications of Hydraulics in environmental engineering. i) To design water distribution system from reservoir. ii) To determine the pressure head of water supply system. iii) To determine the power required for pumps. iv) To measure the pressure at a point. v) To design the pipe diameter of water supply line as well as sewer system. <i>*(Any four Points each 1 Mark each)</i>	*
c) Define ideal fluid and real fluid.	
Ans:- Ideal Fluid:- A fluid, which does not possess viscosity, Surface tension and compressibility is known as ideal fluid.	01
Real Fluid:- A fluid, which possess viscosity, Surface tension and compressibility is known as real fluid.	01

d) State Newton's law of viscosity.	
Ans:- It states that “The shear stress on a layer of a fluid is directly proportional to the rate of shear strain”. $\zeta = (\tau/y) = \mu \times (v/y)$	02
e) A pressure of 1.2 Pascal applied to 650 litres of liquid caused a volume reduction by 1.5 litres. Calculate bulk modulus of elasticity for liquid	
Ans:- Given Data:- $d_p = 1.2 \text{ pa.} = 1.2 \text{ N/m}^2$, $V = 650 \text{ litres}$, $d_v = 1.5 \text{ litres}$ Bulk Modulus = $K = -(dP/(dv/V))$ $= -(1.2/(1.5/650))$ $= - 520 \text{ N/m}^2$	01
	01
f) Define pressure &. State its SI unit.	
Ans:- Pressure at a point due to a liquid is defined as the force acting per unit area. SI unit :- N/m^2	01
	01
g) How will you measure negative pressure?	
Ans:- Mercury in the U-tube is deflected by h_2 due pressure at point A, as deflection occurs in the left limb indicates that, pressure at A is negative (vacuum), pressure above the horizontal datum x-x in the left and right limb of the manometer should be same  <p>Pressure above x-x in the left limb = $S_1 h_2 + S_1 h_1 + P_A$ Pressure above x-x in the right limb = 0 $P_A = - (S_1 h_2 + S_1 h_1)$-----</p>	01
	01
h) Define Reynolds number	
Ans:- The Reynolds number is the ratio of inertia force to the viscous force.	01
$R_N = (\text{Inertia Force/ Viscous Force})$	01
i) Mention necessity of inverted manometer	
Ans:- 1) To measure low and negative pressure differences in two pipes. 2) To measure sensitive pressure	01
	01
j) Write modified Darcy-Weisbach equation	
Ans:- Modified Darcy-Weisbach Equation $hf = \frac{fLQ^2}{12.1 D^5}$	02
k) Define Froude's number	
Ans:- The Froude's number is defined as the square root of the ratio of inertia force of flowing fluid to the gravity force.	02

$$F_e = \sqrt{\frac{F_i}{F_g}}$$

1) List four uses of pitot tube
Ans:-

- i) The pitot tube is a simple and convenient instrument to measure the difference between static, total and dynamic pressure (or head)
- ii) To measure the velocity in channel
- iii) To measure the velocity at a point in flow stream
- iv) Pitot-static tube can measure the fluid flow velocity by converting the kinetic energy in the fluid flow into potential energy

 $\frac{1}{2}$
(each)

Q2. Attempt any FOUR of the following

16

a) State Pascal's law & its practical application
Ans:-

Pascal's Law: - Pascal's Law states that the pressure or intensity of pressure at a point in a static fluid is equal in all directions

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Application: - Law is applied in the construction of machines used for multiplying forces e.g. hydraulic jack, hydraulic pressure, hydraulic lift, hydraulic crane, hydraulic river, etc.

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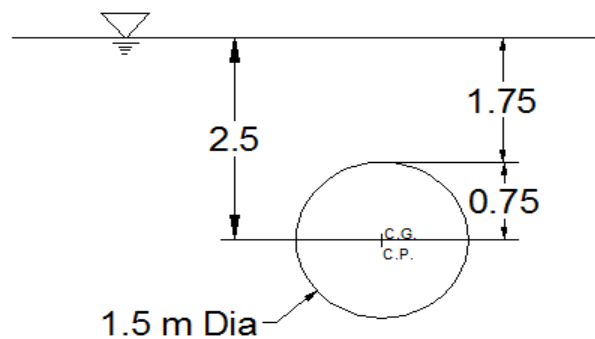
b) A circular plate 1.5 m diameter is placed vertically in water so that the centre plate is 2.5 m below the free surface. Determine the total pressure on the plate and depth of centre of pressure.
Ans:-

Given Data :-

$$d = 1.5 \text{ m}$$

$$x = 2.5 \text{ m}$$

Sketch



Solution :-

$$\begin{aligned} \text{Area} = A &= (\pi/4) \times d^2 \\ &= (\pi/4) \times 1.5^2 = 1.767 \text{ m}^2 \end{aligned}$$

i) Total Pressure on gate

$$F = w \cdot AX$$

$$X = \text{Distance of C.G. from free surface of water} = 2.5 \text{ m}$$

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$$F = 9810 \times 1.767 \times 2.5$$

$$F = 43.34 \times 10^3 \text{ N} = 43.34 \text{ KN}$$

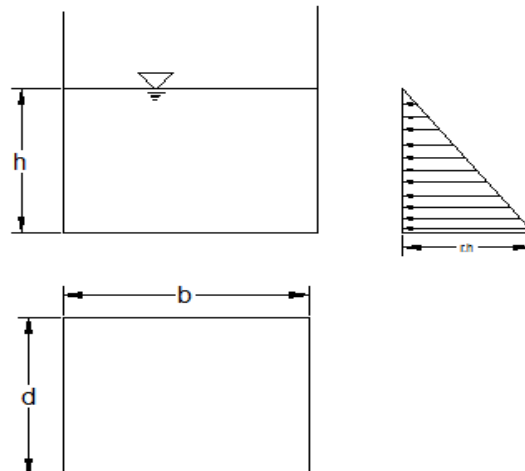
ii) Centre of Pressure.

$$h = X + I.G. / AX$$

$$\text{I.G.} = (\pi/64) \times d^4 = (\pi/64) \times 1.5^4 = 0.2485 \text{ m}^4$$

$$h = 2.5 + [0.2485 / (1.767 \times 2.5)] = 2.5 + 0.0563 = 2.556 \text{ m.}$$

c) Draw a neat sketch of pressure diagram showing variation of pressure on vertical side wall of tank and horizontal bottom of tank containing liquid of specific weight ' γ ' upto a height of ' h '.



The pressure on side of the tank = $\frac{1}{2} \times \gamma h^2$,

The pressure on bottom of the tank = $\gamma h \times \text{plan area of tank}$

d) Convert the pressure of 0.5 N/mm² in metres of liquid of specific gravity 0.7.

$$p = \gamma_L \quad h = S_L \gamma_w \quad h$$

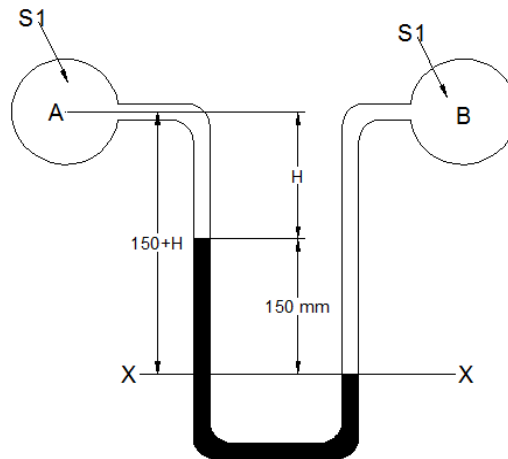
$$0.5 = 0.7 \times 9.81 \times 10^{-6} \times h$$

h = 72812 mm

$$h = 72.812 \text{ m}$$

e) A differential manometer connected at the two points A & B on a horizontal pipe. Carrying specific gravity 0.8 shows a difference in mercury levels as 15 cm. Find the difference in pressure at the two points in of oil and N/m².

Given :- $S_1 = 0.8$, $h = 15 \text{ cm} = 150 \text{ mm}$, $S_m = 13.6$



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The pressure head in the right limb above X-X

$$= h_B + S_1 (H + 150) \text{ mm of water}$$

$$= h_B + S_1 H + 150 S_1 \text{ mm of water.}$$

The pressure head in the left limb above X-X

$$= h_A + S_1 H + S_m \times 150 \text{ mm of water.}$$

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Equating both pressure

$$h_B + S_1 H + 150 S_1 = h_A + S_1 H + S_m \times 150$$

$$h_A - h_B = 150 S_m - 150 S_1$$

$$= 150(S_m - S_1)$$

$$= 150(13.6 - 0.8)$$

$$= 1920 \text{ mm of water} = 1.92 \text{ m of water}$$

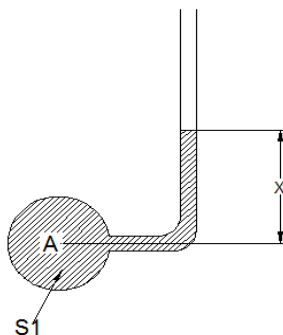
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$$\text{Difference of pressure} = w(h_A - h_B) = 9810 \times 1.92 = 18.835 \times 10^3 \text{ N/m}^2$$

f) What is Piezometer and where it is used?

Piezometer:- A piezometer tube is the simplest form of instrument, used for measuring moderate pressures. It consists of a tube one end of which is connected to the pipe line in which the pressure is required to be found out. The other end is open to the atmosphere in which the liquid can rise freely without overflow. The height to which the liquid rises up in the tube gives the pressure head directly.

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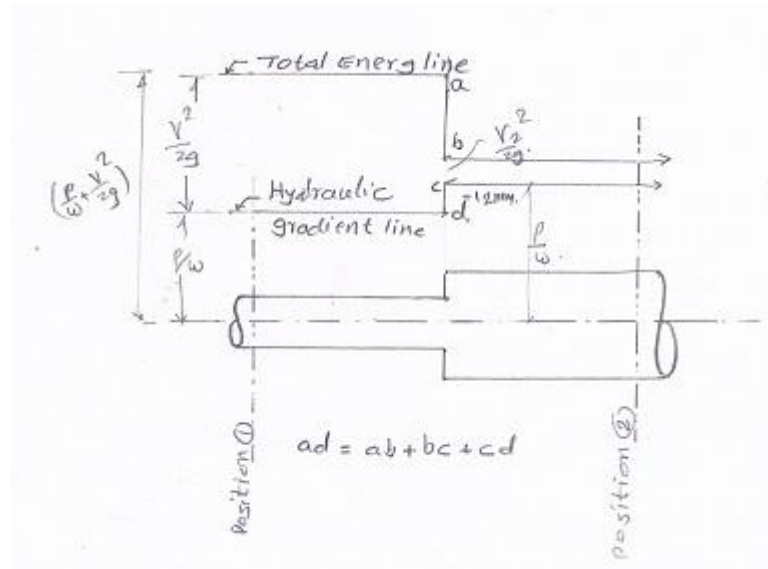
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Use:- To measure pressure at a point in the pipe.

e) At a sudden enlargement of water line a 250 mm diameter to 500 mm diameter pipe, the hydraulic gradient uses. by 12 mm Calculate the discharge through pipe.

Ans:-



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Let, v_1 = velocity of water at section 1,

v_2 = velocity of water at section 2,

Let us draw hydraulic gradient line and total energy line above center line of pipe as below .

From the equation of continuity

$$a_1 v_1 = a_2 v_2$$

$$= \frac{\pi}{4} \times (250)^2 \times v_1 = \frac{\pi}{4} \times (500)^2 \times v_2$$

Therefore

$$v_1 = 4v_2$$

Now from the geometry of figure above

$$Ad = ab + bc + cd$$

$$(v_1)^2/2g = (v_1 - v_2)^2/2g + (v_2)^2/2g + 12 \text{ mm}$$

$$(4v_2)^2/2g = (4v_2 - v_2)^2/2g + (v_2)^2/2g + 12 \text{ mm}$$

$$= (16(v_2)^2)/2g = (9(v_2)^2)/2g + (v_2)^2/2g + 12 \text{ mm}$$

$$= (v_2)^2 = (12 \times 9.81 \times 1000) / 3$$

$$= (v_2) = 198.09 \text{ mm/Sec}$$

Therefore

$$Q = a_2 \times v_2$$

$$= \pi/4 \times (500)^2 \times 198.09$$

$$= 38894880.55 \text{ mm}^3/\text{Sec}$$

$$= 38894880.55 / (10)^6 = 38.895 \text{ lit/Sec.}$$

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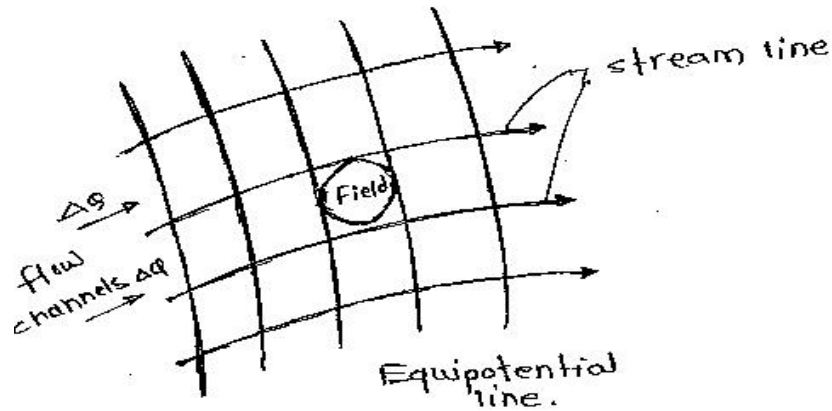
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f) What is flow net ' State applications of flow net.

Flow net: Flow net is the graphical method of seepage analysis. The method of flow net construction is based on trial sketching. It is graphical presentation of stream lines & equipotential lines. A set of stream line and equipotential lines constitute a flow net. The flow lines & equipotential lines meet at right angles to one another. The fields are approximately squares, so that circle can be drawn touching all four sides of the square.

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Applications of flow net:- 1) In seepage analysis of dam foundation
2) In seepage analysis of body of dam ,
3) In the design of hydraulic structures.

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Q4. Attempt any FOUR of the following.

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a) Define friction factor & state any four factors affecting friction factor.

Friction Factor :- A dimension less quantity depends upon the roughness inside the pipe ,viscosity of liquid flowing throw pipes which affect's head loss is known as Friction Factor.

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factors affecting friction factor:- (ANY TWO)

- 1) Nature of Surface of Pipe material
- 2) Pipe diameter
- 3) Length of pipeline
- 4) Head loss
- 5) Square of Velocity of flow

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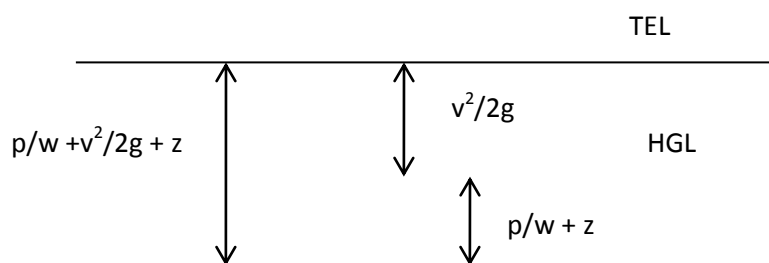
b) Explain HGL and TEL with curve.

Hydraulic Gradient Line (HGL): It is the line which gives the sum of pressure head (p/w) and datum head (z) of a flowing fluid in a pipe with respect to some reference line .Hydraulic gradient line is obtained by joining the top of all vertical ordinates, showing the pressure head (p/w) of flowing fluid in a pipe from the center of the pipe.

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Total Energy Line(TEL):): It is the line which gives the sum of pressure head(p/w),datum head(z) and kinetic head($v^2/2g$) of a flowing fluid in a pipe with respect to some reference line .Total energy line is obtained by joining the tops of all vertical ordinates, showing the pressure head(p/w) and kinetic head($v^2/2g$) of flowing fluid in a pipe from the center of the pipe.

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c) What do you mean by water hammer ' State its causes (any three)	
<p>Ans:-</p> <div data-bbox="592 283 1193 472" data-label="Diagram"> </div> <p>Water Hammer-When the water flowing in a long pipe is suddenly brought to rest by closing the valve, there will be a sudden rise in pressure due to the momentum of the moving water being destroyed. This causes a wave of high pressure to be transmitted along the pipe which creates noise known as water hammer .The rise in pressure in some cases may be so large that the pipe may even burst. Therefore it is essential to take into account this pressure rise in the design of pipes. The magnitude of pressure rise depends on the speed at which the valve is closed, velocity of flow, length of the pipe and elastic properties of the pipe material as well as flowing fluid.</p> <p>Causes.</p> <p>If a fluid flowing in a pipe is suddenly brought to rest by closing the valve, there will be sudden rise in pressure due to momentum of the moving fluid being destroyed.</p> <ol style="list-style-type: none"> 1) This causes a series of pressure vibrations. 2) These vibrations setups noises in the pipe. 	<p>02</p> <p>02</p>
d) A diameter of a horizontal pipe suddenly changes from 25 cm to 30 cm. Calculate the loss of head, if discharge is 370 lit/sec	
<p>Ans:-</p> <p>$Q=0.37\text{m}^3/\text{Sec}$</p> <p>$D_1=.25\text{ m} ,d_2=0.30\text{ m} ,$</p> <p>$A_1=(\pi/4 \times (0.25)^2)=0.049\text{ m}^2$</p> <p>$A_2=(\pi/4 \times (0.30)^2)=0.0707\text{ m}^2$</p> <p>$V_1=(0.37/0.049)=7.5510\text{ m/Sec}$</p> <p>$V_2=(0.37/0.0707)=5.2333\text{ m/Sec}$</p> <p>Head loss $= (v_1-v_2)^2/2g = (7.5510-5.2333)^2/2 \times 9.81$</p> <p>$=0.2737\text{ m}$</p>	<p>01</p> <p>01</p> <p>01</p> <p>01</p>
e) Two reservoirs having a difference in elevation of 15 in connected by a 200 mm diameter siphon. The length of the siphon is 400 in the summit is 3 in the water level in the upper reservoir. The length of the pipe from upper reservoir to the summit is 120 mm. Determine the discharge through siphon, if the coefficient of friction is 0.005.	
<p>Ans:-</p> <p>Difference in elevation between two reservoir =15 m</p> <p>Diameter of siphon =D=0.2 m</p> <p>length of siphon=L=400 m</p> <p>coefficient of friction = f = 0.005</p> <p>Neglecting minor losses at entry and exit</p>	

<p>Total head = frictional head =</p> $H = hf = (fLv^2)/2 \times g \times D$ $15 = (0.005 \times 400 \times v^2)/(2 \times 9.81 \times 0.2)$ $V = 2.765 \text{ m/Sec}$ <p>Discharge = $Q = (\pi/4 \times (D)^2) \times v$</p> $Q = (\pi/4 \times (0.2)^2) \times 2.765$ $Q = 0.0868 \text{ m}^3/\text{Sec}$ $Q = 86.86 \text{ lit/Sec}$	01
<p>f) Water is flowing through a rectangular channel of width 8 in bed slope 1 in 1000. Depth of flowing channel is 5 in. Find the discharge through the channel. Take Chezy's constant C = 50.</p>	
<p>Ans:-</p> $A = (8 \times 5) = 40 \text{ m}^2$ $Q = (a \times v)$ <p>Using chezy's formula,</p> $V = c\sqrt{mi}$ <p>m=hydraulic mean depth = A/p</p> <p>i= bed slope =1 in 1000 =0.001, c= chezy's constant =50</p> $p = (b+2d) = (8+2 \times 5) = 18 \text{ m}$ <p>m=hydraulic mean depth = A/p=(40/18)=2.22</p> $Q = (a \times c\sqrt{mi}) = (40 \times 50 \times \sqrt{(2.22 \times 0.001)})$ $Q = 94.2337 \text{ m}^3/\text{Sec}$ $Q = 94233.7 \text{ lit /Sec}$	01
<p>Q5. Attempt any TWO of the following:</p>	16
<p>a) A trapezoidal channel section has side slope 2 vertical to 3 horizontal. It is discharging water at a rate of 20 cumecs with bed slope 1 in 2000. Design the channel for its best form. Take Manning's constant 0.01.</p>	
<p>Ans:-</p> <p>Type of channel : trapezoidal channel , Side slope of channel =3H: 2V, Discharge =Q= 20 cumecs = 20 m³/sec ,Bed slope = i=1 in 2000 =1/2000 ,Mannigs constant =N=0.01</p> <p>Let ,b = base width of channel , d = depth of flow</p> <p>Side slope 3H:2V n/1=3/2 n=3/2</p> <p>Trapezoidal channel is designed for best form, We have condition</p> $d \sqrt{(n^2+1)} = 1/2(b+2nd)$ $d \sqrt{[(3/2)^2 + 1]} = 1/2[b+2 \times (3/2) \times d]$ $1.80 d = 0.5b + 1.5d$ $0.3d = 0.5b$ <p>b =0.6 d</p> <p>Put the value of b in below eqn,</p> $A = (b+ nd) d$ $A = [0.6d + (3/2) \times d]d$ $A = 2.1 d^2$	01
	01
	01

$$\begin{aligned}\text{Wetted perimeter} = P &= 2d \sqrt{(n^2+1)} + b \\ &= 2d \sqrt{[(3/2)^2 + 1]} + 0.6d \\ &= 4.205d\end{aligned}$$

$$\begin{aligned}\text{Hydraulic radius} = R &= A/P \\ &= 2.1d^2 / 4.205d = 0.499d = 0.5d\end{aligned}$$

Manning's formula

$$Q = A \times 1/N \times R^{2/3} \times i^{1/2}$$

$$20 = 2.1d^2 (1/0.01) \times (0.5d)^{2/3} \times (1/2000)^{1/2}$$

d = depth of flow = 2.36 m

b = base width of channel = 0.6 d = 0.6 x 2.36 = 1.42 m

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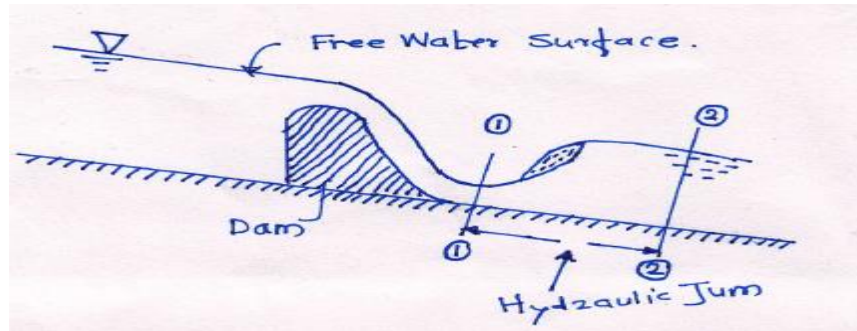
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b) What do you mean by Hydraulic Jump? Explain with sketch. State the types of hydraulic jump with Froude's number.

Ans:-



02

Hydraulic Jump:-

Consider the flow of water over a dam. The height of water at section 1-1 is small; as we move toward downstream the height or depth of water increases rapidly over a short length of the channel. This is because at the section 1-1 is less than critical depth. Shooting flow is an unstable type of flow and does not continue on the downstream side. Then this shooting will convert itself into a streaming flow & hence depth of water will increase. This sudden increase of depth of water is called a hydraulic jump.

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OR when supercritical flow changes to subcritical then sudden rise of water occurs, this sudden increase of depth of water is called a hydraulic jump.

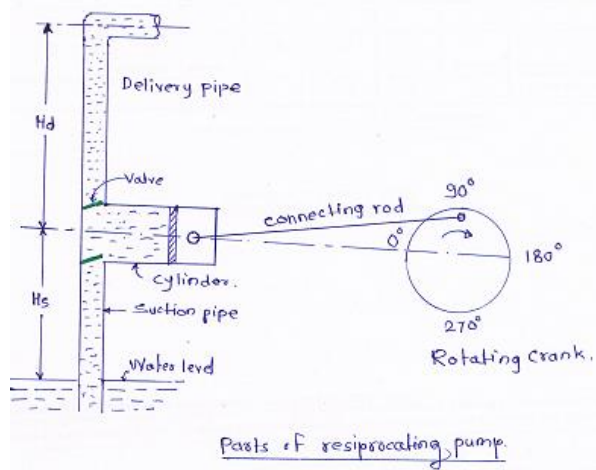
Types of flow with Froude's number (Fe) number:-

- 1) Critical flow, $Fe = 1$
- 2) Subcritical flow or streaming flow, $Fe < 1$
- 3) Super Critical or Shooting flow, $Fe > 1$

**(Note :-Instead of types of hydraulic jump consider types of flow)*

02

c) A 150 mm x 75 mm venturimeter placed vertically with the throat 22.5 mm above the inlet conveys oils of specific gravity 0.78 at 29 litres per sec. Calculate the difference of pressure between inlet and throat Take $C_d = 0.96$.



Component part and its function -

- Cylinder:-To guide movement of piston and create negative and positive pressure.
- Section pipe:-To connect source of water and the cylinder
- Delivery pipe:-To receive water from cylinder and discharge it at outlet
- Valve:-To admits flow from the suction pipe into the cylinder and from cylinder into delivery pipe.
- Rotating crank:-To give linear displacement to connecting rod.
- Connecting rod:-To connects the piston and the rotating crank.

*** Note :- (Diagram 2 marks ,labelling 2 marks, any four component with function 4 marks)**

b) A horizontal venturimeter is installed in a pipe of 20 cm diameter carries 50 lps of water with a differential mercury manometer reading of 12.6 cm. Calculate the throat diameter in metre. Assume' coefficient of meter is 0.98.

Ans:-

Given data.

Diameter at inlet = $d_1 = 20 \text{ cm} = 0.2 \text{ m}$

Diameter at throat = $d_2 = ?$

Monometer reading = $x = 12.6 \text{ cm} = 0.126 \text{ m}$.

Coefficient of meter = $C_d = 0.98$

Discharge through venturimeter = $Q = 50 \text{ lps} = 50 \times 10^{-3} \text{ m}^3/\text{s}$

a_1 = area at inlet of venturimeter.

$$= \frac{\pi}{4} d_1^2 = \frac{\pi}{4} \times (0.2)^2 = 3.14 \times 10^{-2} \text{ m}^2$$

a_2 = area at throat of venturimeter,

$$h = x \left[\frac{S_m}{S_w} - 1 \right]$$

$$h = 0.126 \left[\frac{13.6}{1} - 1 \right]$$

$$= 0.126 \times 12.6$$

$$= 1.5876 \text{ m of water}$$

$$Q = C_d \times \frac{a_1 a_2}{\sqrt{a_1^2 - a_2^2}} \times \sqrt{2gh}$$

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$Q = Cd \times \frac{a_1}{\sqrt{\left(\frac{a_1}{a_2}\right)^2 - 1}} \times \sqrt{2gh}$	01
$50 \times 10^{-3} = 0.98 \times \frac{3.14 \times 10^{-2} \times a_2}{\sqrt{(3.14 \times 10^{-2})^2 - (a_2)^2}} \times \sqrt{2 \times 9.81 \times 1.5876}$	02
$a_2 = 8.777 \times 10^{-3} \text{ m}^2$	
$a_2 = \frac{\pi}{4} d_2^2$	
$8.777 \times 10^{-3} = (3.14/4) \times d_2^2$	02
$d_2 = \text{Diameter of throat} = 0.1057 \text{ m}$	
c) Why triangular notches are preferred than rectangular notches? Find the discharge over the triangular notch of angle 60° when the head over the notch is 20 cm. Take $Cd = 0.625$.	
Triangular notches are preferred than rectangular notches because :-	
1) Only one reading i.e head (H) is required to be taken for measurement of rate of flow in a given triangular notch.	01
2) If in triangular notch the angle of the notch i.e. $\theta = 90^\circ$, the formula become very simple to remember.	01
3) A triangular notch gives more accurate result for low rate of flow than a rectangular notch.	01
4) The same triangular notch can measure a wide range of flows accurately.	01
Given data;- Type of notch = triangular Angle of notch = $\theta = 60^\circ$ Head over notch = $H = 20 \text{ cm} = 0.20 \text{ m}$ Coefficient of discharge = $Cd = 0.625$ Discharge = $Q = ?$ For triangular notch discharge can be calculated by using formula.	
$Q = \frac{8}{15} C_d \sqrt{2g} \tan \frac{\theta}{2} \times H^{5/2}$	02
$= \frac{8}{15} \times 0.625 \times \sqrt{2 \times 9.81} \times \tan (60/2) \times (0.20)^{5/2}$	
$= 0.01525 \text{ m}^3/\text{sec}$	
Discharge over triangular notch = $0.01525 \text{ m}^3/\text{sec}$.	02